Mathematical Finance Dylan Possamaï

## Recall 5

## Abstract financial markets

- 1. What is the set of *m*-admissible  $(\mathbb{F}, \mathbb{P})$ -wealth processes?
- 2. Let m > 0. Let  $\mathcal{X}_m(\mathbb{F}, \mathbb{P})$  be a set of *m*-admissible  $(\mathbb{F}, \mathbb{P})$ -wealth processes. Let  $(X, X^1, X^2) \in \mathcal{X}_1(\mathbb{F}, \mathbb{P}) \times \mathcal{X}_2(\mathbb{F}, \mathbb{P}) \times \mathcal{X}_3(\mathbb{F}, \mathbb{P})$ . Can you give two stability properties? Can you prove them?
- 3. Can you give an example of a set of *m*-admissible  $(\mathbb{F}, \mathbb{P})$ -wealth processes?

## On arbitrage opportunities and the first FTAP

- 1. Can you state the condition of absence of arbitrage (NA)?
- 2. Can you state the condition of no-free lunch (NFL)?
- 3. Can you state the condition of no-free lunch with vanishing risk (NFLVR)?
- 4. Can you state the condition of no-free lunch with bounded risk (NFLBR)?
- 5. Can you state the condition of no-unbounded profit with bounded risk (NUPBR)?
- 6. When is an  $\mathcal{F}_T$ -measurable random variable  $\xi$  called an arbitrage of the first kind?
- 7. Can you state some equivalences between conditions?
- 8. Can you state some inclusions between conditions?
- 9. Can you give two equivalent statements to " $\mathcal{X}(\mathbb{F},\mathbb{P})$  satisfies Condition (NFLVR)"? Can you prove it?

## No-free lunch and Kreps-Yan's theorem

- 1. Can you state the Kreps–Yan's theorem? Can you prove it?
- 2. Can you state the Equivalence Separating Measure Condition (ESM)?
- 3. To which condition is (ESM) equivalent? Can you prove it?
- 4. Can you give three relations between Condition (ESM) and the sets  $\mathcal{M}_{\sigma}(S, \mathbb{F}, \mathbb{P})$ ,  $\mathcal{M}_{\text{loc}}(S, \mathbb{F}, \mathbb{P})$  and  $\mathcal{M}(S, \mathbb{F}, \mathbb{P})$ ? Can you prove them?